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# EXPERIMENTAL WIRELESS CHANNEL MODEL DERIVATION

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**Sergey D. Andreev**

State University of  
Aerospace Instrumentation (SUAI)  
[Serge.Andreev@gmail.com](mailto:Serge.Andreev@gmail.com)

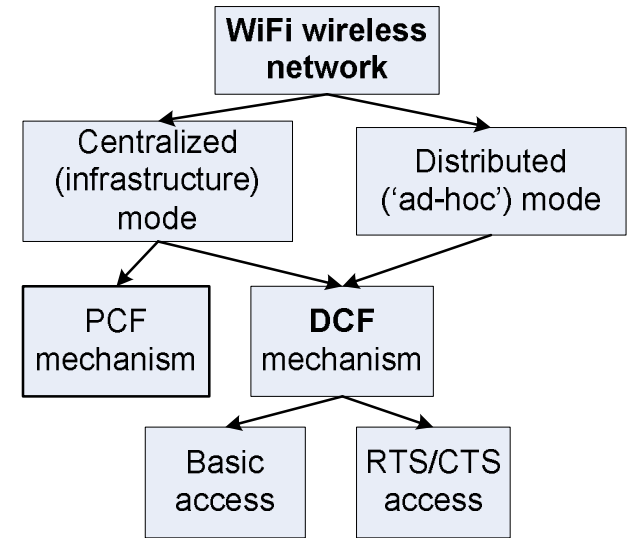
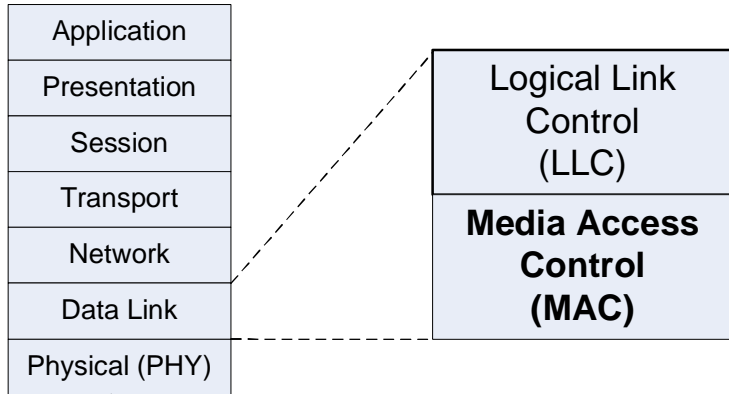
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# Session Outline

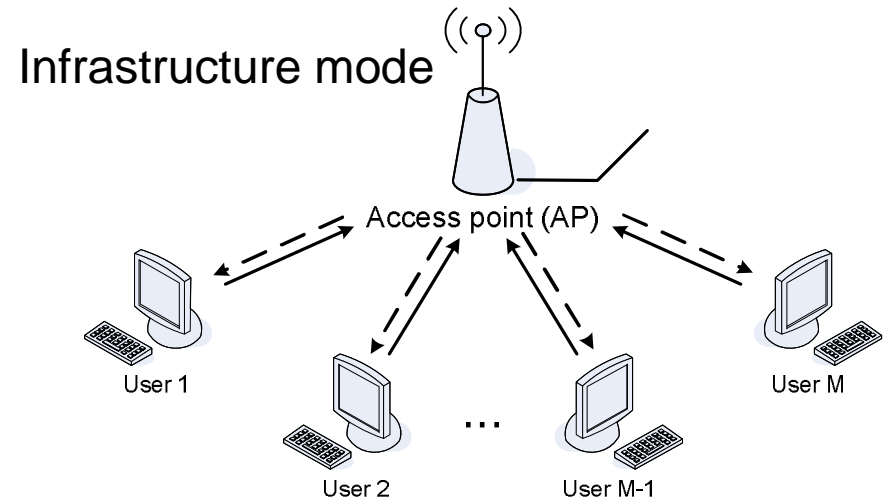
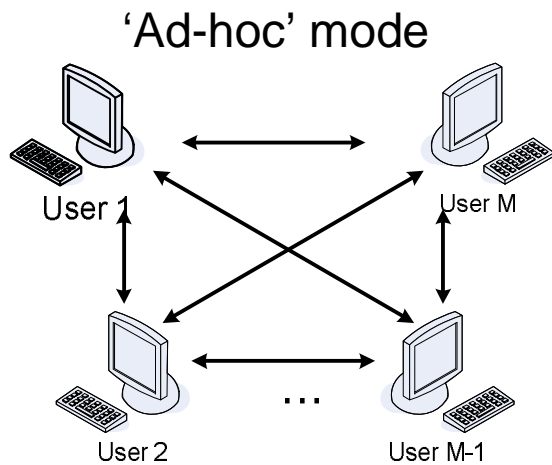
- n Research Focus
- n MAC Throughput Measurement
- n Packet Error Rate Measurement
- n Hidden Markov Models Summary
- n Appropriate State Space Selection
- n 2-state Model Description  
and Parameters Derivation
- n Conclusion

# Research Focus

## OSI Layers

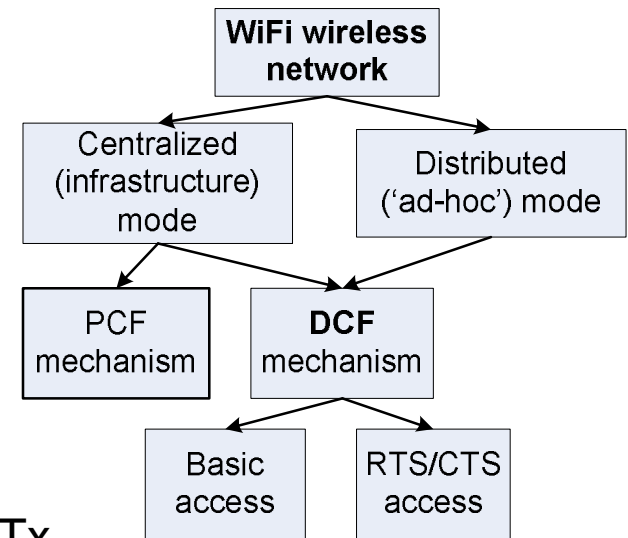


Consider IEEE 802.11g (WiFi) telecommunications standard

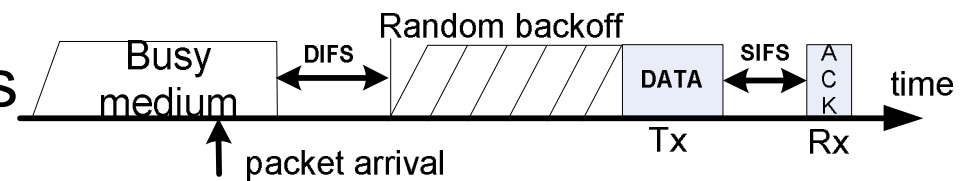


# DCF Mode Operation

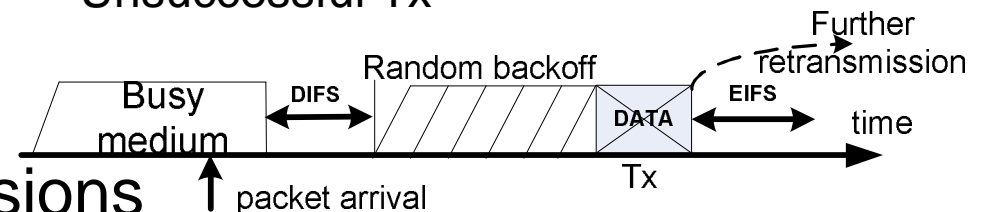
- n Distributed Coordination Function (DCF) is a **randomized** channel access **scheme**
- n **Packet corruption** and **collisions** are handled by Automatic Repeat reQuest (ARQ) mechanism that relies on packet **retransmission**
- n Retransmission **obscures** real channel situation for the upper layers as the actual number of retransmissions is a **random variable**



Successful Tx



Unsuccessful Tx



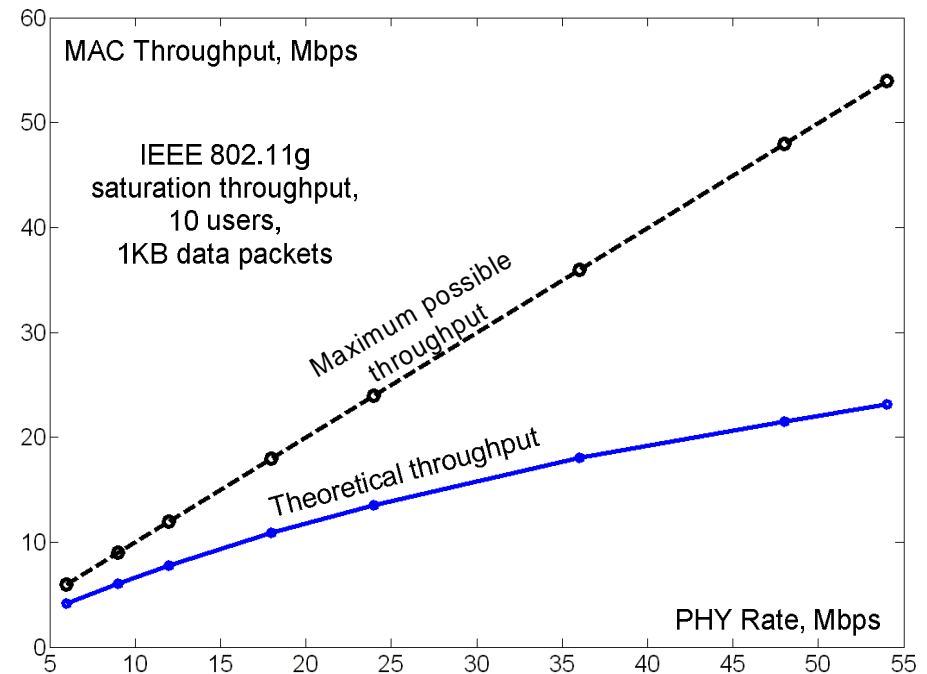
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# Problem Statement

- n **Measure IEEE 802.11g MAC throughput** with high time resolution (required for real-time video transmission modeling)
  - n **Obtain mean packet error rate** without packet retransmission
  - n **Collect realistic packet error traces**
  - n **Build appropriate error source model** (required to calculate transport coding parameters)
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# Expected MAC Throughput

- n Follow Bianchi (2000) approach to calculate **throughput in saturation conditions**
- n **Gap** between PHY rate and MAC throughput **increases** as rate grows

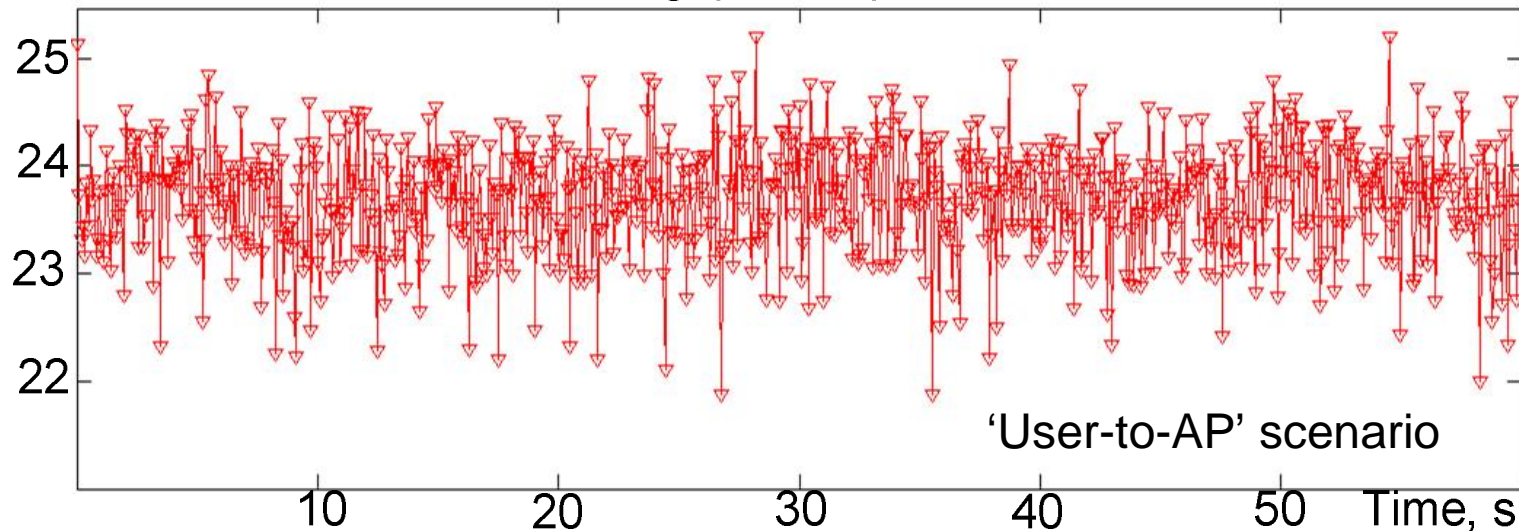
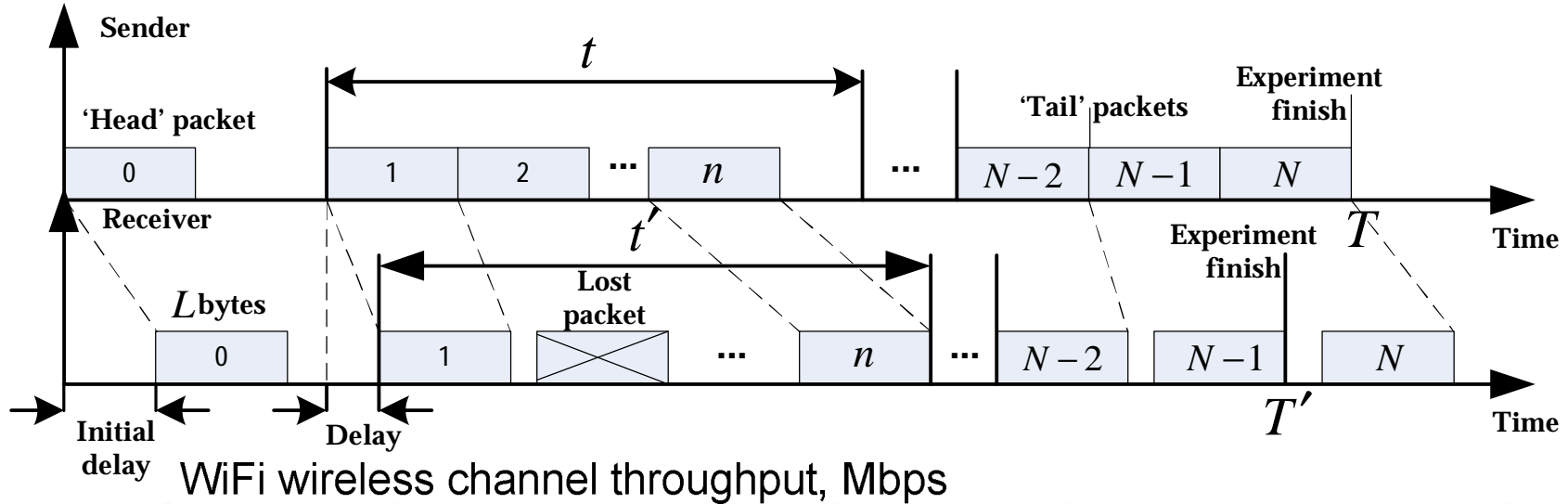


## Main considerations

- n To measure actual throughput adequately **retransmission should be disabled!**
- n Existing tools are **incapable** of measuring throughput with **high time resolution\***

\* see discussion in S. Andreev, S. Semenov, A. Turlikov "Methods of estimation of radiochannel parameters", 2007

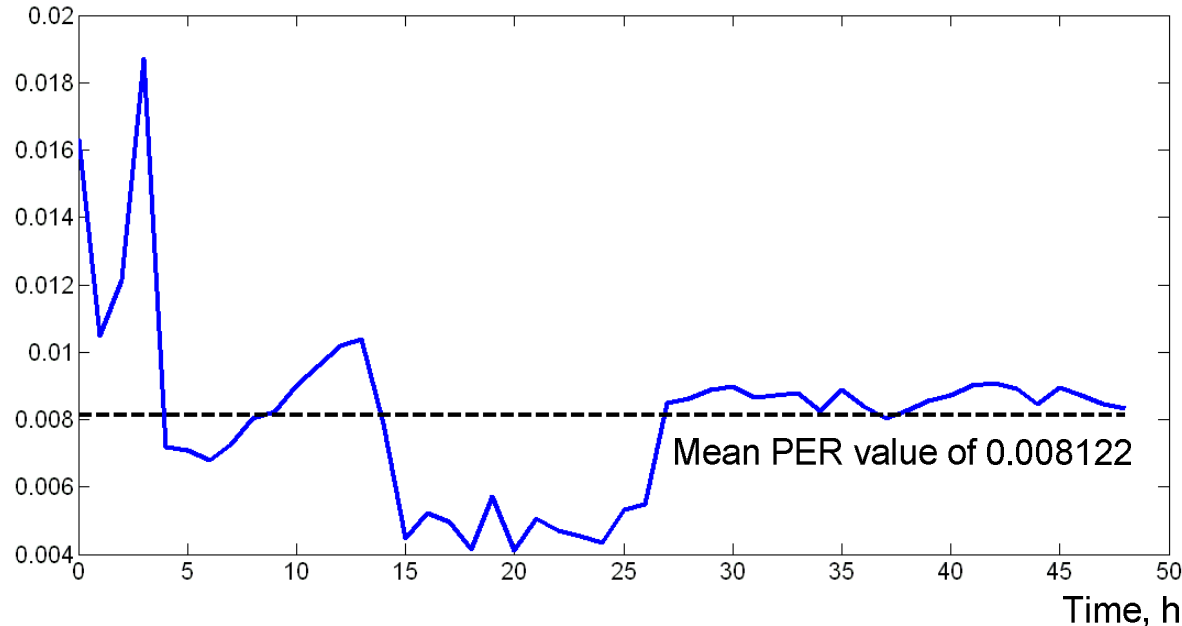
# Proposed Measuring Methodology



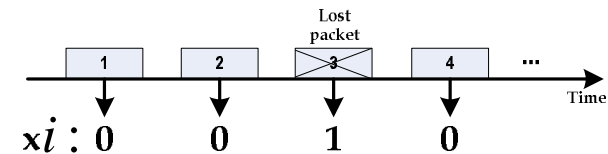
Measured throughput accords with Bianchi theoretical estimation!

# Packet Error Rate (PER) Measurement

WiFi PER value



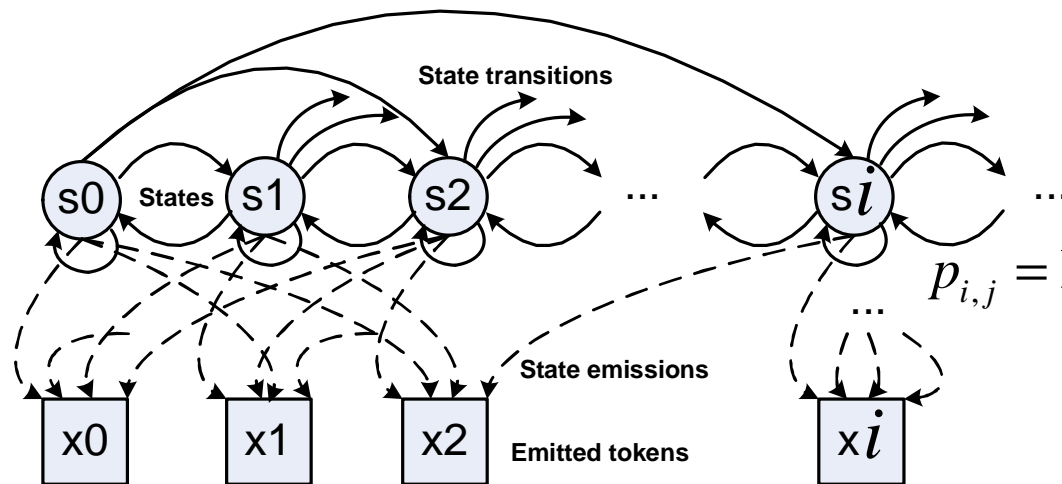
Packet error trace



- n Average PER with disabled retransmission is **below 1%**
- n A model is needed to **describe PER behavior** for realistic **packet error traces**
- n Main target: maintain **simplicity – precision balance**
- n Renown technique is to use Hidden Markov Models (**HMM**)



# Hidden Markov Model (HMM) Summary



Given by **transition** and **emission** probability matrices

$$p_{i,j} = \Pr\{s_{t+1} = j \mid s_t = i\} = \begin{bmatrix} p_{1,1} & p_{1,2} & \dots \\ p_{2,1} & p_{2,2} & \dots \\ \dots & \dots & \dots \\ e_{1,1} & e_{1,2} & \dots \\ e_{2,1} & e_{2,2} & \dots \\ \dots & \dots & \dots \end{bmatrix}$$

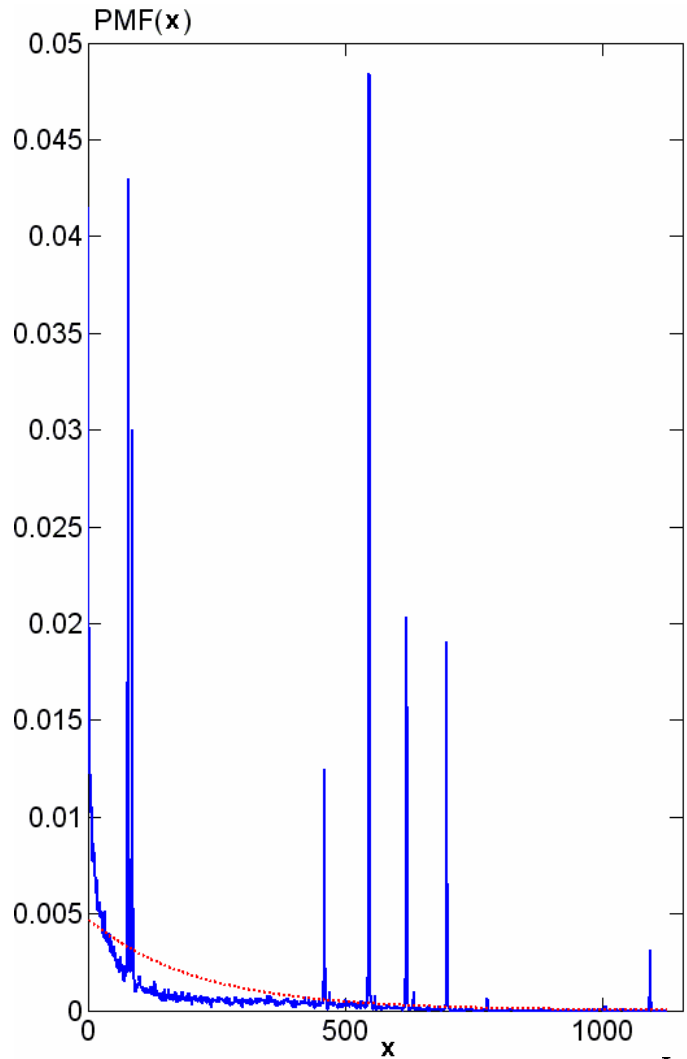
$$e_{i,j} = \Pr\{x_t = j \mid s_t = i\} = \begin{bmatrix} e_{1,1} & e_{1,2} & \dots \\ e_{2,1} & e_{2,2} & \dots \\ \dots & \dots & \dots \end{bmatrix}$$

## Canonical problems

- n Compute the probability of a particular output sequence for known parameters (forward-backward algorithm)
- n Find the most likely sequence of hidden states for known parameters (Viterbi algorithm)
- n **Find the most likely set of state transition and emission probabilities** given an output sequence of  $x_i$  (Baum-Welch algorithm\*)

\* is **highly complex** and requires initial estimates of the transition and emission matrices

# Binary Symmetric Channel (BSC) Assumption

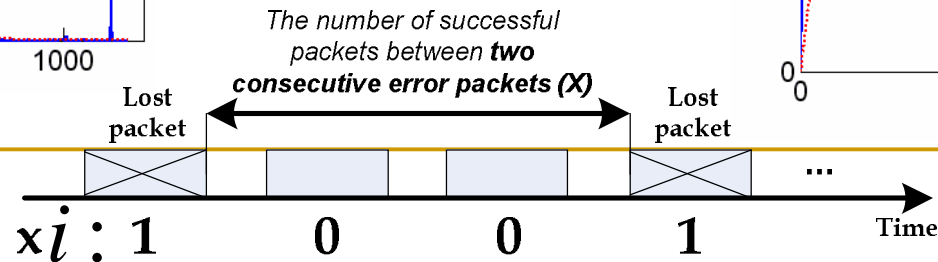
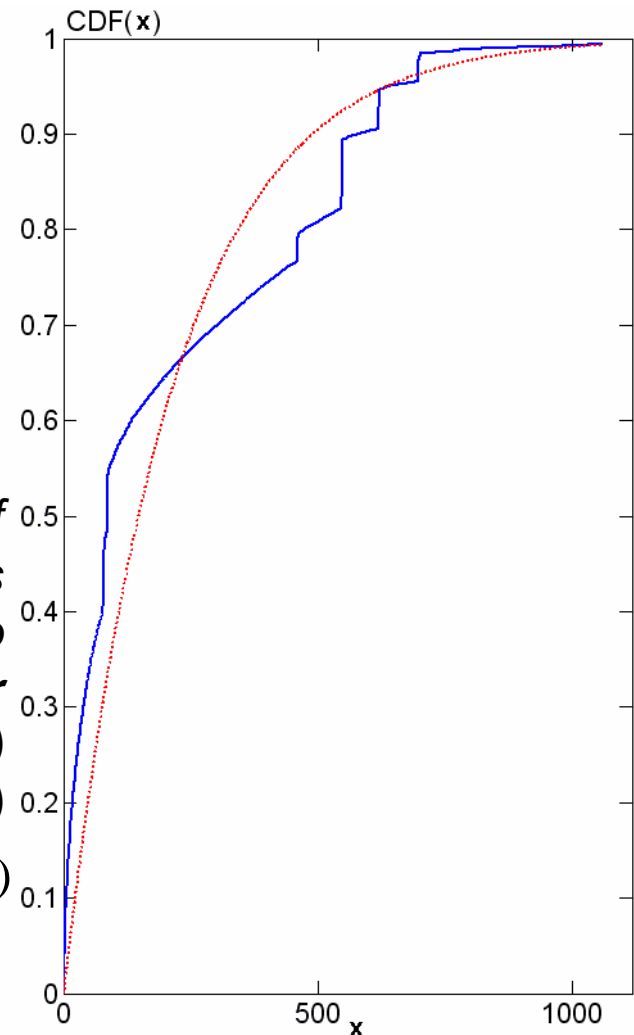


PMF for the number of successful packets between **two consecutive error packets**: theory (dotted) and practice (solid)

$$PMF(x) = \begin{cases} \Pr(X = x), & x \in S \\ 0, & x \in R \setminus S \end{cases}$$

CDF for the number of successful packets between **two consecutive error packets**: theory (dotted) and practice (solid)

$$CDF(x) = \Pr(X \leq x)$$



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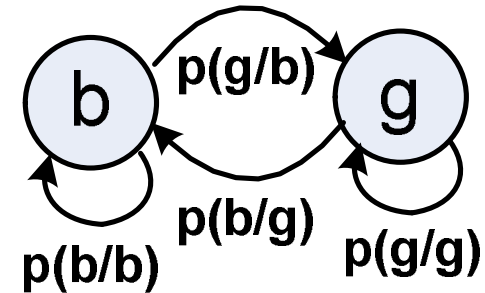
# Previous Models

- n Bit level models (PHY bit inversion probability)
    - q Gilbert model, 1960
    - q Gilbert-Elliott model, 1963
    - q Wang et al., Zorzi et al., 1995-96  
(relevance of the 2-state model)
    - q Lyakhov et al., 2004  
(2-state model for WiFi **with retransmissions**)
  
  - n Packet level models (Use with **packet error traces**)
    - q Zorzi et al., 1997  
(2-state model is good at packet level)
    - q Giao et al., Konrad et al., 1996-2001 (realistic data)
    - q Wang et al., 1995 (larger Markov chain state space)
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# 2-state HMM Definition

- Markov chain transition probabilities:

$$P = \begin{bmatrix} p(g/g) & p(b/g) \\ p(g/b) & p(b/b) \end{bmatrix}$$



- Matrix 2-state model:

$$A(0) = \begin{bmatrix} q_g p(g/g) & q_b p(b/g) \\ q_g p(g/b) & q_b p(b/b) \end{bmatrix} \quad A(1) = \begin{bmatrix} p_g p(g/g) & p_b p(b/g) \\ p_g p(g/b) & p_b p(b/b) \end{bmatrix} \quad \begin{array}{l} \bar{a}_0 = (p(g), p(b)) \\ \bar{b}_0 = (1, 1)^T \end{array}$$

- Probability of a given error sequence:

$$p(\bar{e}) = p(e_1, e_2, \dots, e_n) = \bar{a}_0 \prod_{i=1}^n A(e_i) \cdot \bar{b}_0 \quad \text{instead of}$$

$$p(\bar{e}) = \sum_{s_0} \sum_{s_1} \dots \sum_{s_n} p(s_0) \cdot p(s_1 | s_0) \cdot p(e_1 | s_1) \cdot \dots \cdot p(s_n | s_{n-1}) \cdot p(e_n | s_n)$$

- Easy way to calculate  $P(m, n)$  characteristics

# Model Parameters Derivation

n Denote  $0^i$  and  $1^j$  the sequences of  $i$  zeros and  $j$  ones:

$$a_{00} = \frac{p^2(0^2) - p(0)p(0^3)}{p(0^2) - p^2(0)} \quad a_{01} = \frac{p(0^3) - p(0)p(0^2)}{p(0^2) - p^2(0)} \quad A = 1 + \frac{a_{00} - a_{10}}{a_{11} + a_{01} - 1}$$

$$a_{10} = \frac{p^2(1^2) - p(1)p(1^3)}{p(1^2) - p^2(1)} \quad a_{11} = \frac{p(1^3) - p(1)p(1^2)}{p(1^2) - p^2(1)} \quad B = \frac{-a_{10}}{a_{11} + a_{01} - 1}$$

n The **resulting expressions\*** for the 2-state model:

$$p_b = \frac{A + \sqrt{A^2 - 4B}}{2} \quad p_g = \frac{A - \sqrt{A^2 - 4B}}{2} \quad p(g/g) = 0.9999$$

$$p(b/b) = \frac{(a_{11} + a_{01})p_g - a_{11}}{p_g - p_b} \quad p(g/g) = \frac{a_{11} - p_b(a_{11} + a_{01})}{p_g - p_b} \quad p_g = 0.0044$$

$$p_b = 0.5423$$

\* see discussion in S. Andreev, A. Vinel "Gilbert-Elliott Model Parameters Derivation for the IEEE 802.11 Wireless Channel", 2007

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# Conclusion

## n Achievements

- q A method to measure MAC throughput with high time resolution is introduced
- q Realistic packet error traces of IEEE 802.11g are obtained
- q Appropriate hidden Markov model selection is addressed
- q 2-state wireless experimental model is built
- q The results are published in 2 articles during 2007

## n Open problems

- q Perform goodness-of-fit check of a introduced model
- q Account for 'peaks' in the experimental PMF
- q Compare the derived model with alternatives  
(e. g. D. Moltchanov "Cross-layer performance evaluation and control of wireless channels in NG All-IP networks", Ph.D. thesis, 2006)

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# Discussion